

## Crystal structure of the compound Pr<sub>4</sub>Ge<sub>7</sub>

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The structure of the binary germanide Pr<sub>4</sub>Ge<sub>7</sub> has been determined by single-crystal X-ray diffraction on a twinned crystal. It is an ordered vacancy derivative of the  $\alpha$ -ThSi<sub>2</sub> type, Pearson symbol *oS44*, space group *C222*<sub>1</sub>,  $a = 6.007(2)$ ,  $b = 13.987(4)$ ,  $c = 12.009(4)$  Å, isotypic to the structure reported earlier for Nd<sub>4</sub>Ge<sub>7</sub>. The cell parameters of seven other praseodymium germanides observed in samples annealed at 873 K were refined from powder X-ray diffraction data.

Germanide / Praseodymium / Single-crystal X-ray diffraction / Crystal structure / Vacancy derivative

### Introduction

According to the phase diagram [1-3], eight binary compounds form in the Pr-Ge system: Pr<sub>3</sub>Ge, Pr<sub>5</sub>Ge<sub>3</sub>, Pr<sub>4</sub>Ge<sub>3</sub>, Pr<sub>5</sub>Ge<sub>4</sub>, PrGe (CrB), PrGe (FeB), PrGe<sub>2-x</sub>, and PrGe<sub>2</sub>. The crystal structures of the compounds containing less than 60% Ge are well established, however, the literature data gathered in Table 1 reveal a more complex situation in the Ge-rich part of the system. The stoichiometric compound PrGe<sub>2</sub> mentioned above is probably identical with PrGe<sub>1.91</sub> [13], which crystallizes with a structure related to the TbGe<sub>2</sub> type.

According to Eremenko *et al.* [2] the non-stoichiometric digermanide PrGe<sub>2-x</sub> exists in the range 60.8-62.7 at.% Ge and undergoes a transition at 548-615°C from a tetragonal high-temperature phase with an  $\alpha$ -ThSi<sub>2</sub>-type structure to an orthorhombic room-temperature phase with an  $\alpha$ -GdSi<sub>2</sub>-type structure. Schobinger-Papamantellos *et al.* [9] observed a tetragonal phase with significant change of cell parameters at compositions near PrGe<sub>1.7</sub>. The superstructure observed in a sample PrGe<sub>1.60</sub> was refined in space group *Fdd2*. Boutarek *et al.* [11] reported the coexistence of two tetragonal phases with different *c/a* ratios, called Q<sub>1</sub> and Q<sub>2</sub>, in a sample PrGe<sub>1.74</sub>. The former was found to be single phase at PrGe<sub>1.58</sub>, the latter at PrGe<sub>1.8</sub>. In a later work [10] a sample of composition PrGe<sub>1.6</sub> contained a majority phase, identified as Q<sub>1</sub>, with partly ordered vacancies, which was refined in the orthorhombic Y<sub>3</sub>Ge<sub>5</sub>

structure type [14], and a minority  $\alpha$ -ThSi<sub>2</sub>-type phase Q<sub>2</sub> with disordered vacancies. Venturini *et al.* [12,15] carried out a systematic study of non-stoichiometric digermanides of the rare earths and several structural models with ordered Ge vacancies derived from the  $\alpha$ -ThSi<sub>2</sub> type were proposed, among which the orthorhombic structure type Nd<sub>4</sub>Ge<sub>7</sub>.

Here we present data for binary Pr-Ge compounds obtained during investigations of the Pr-Ag-Ge and Pr-Al-Ge ternary systems [16,17].

### Experimental

Binary Pr-Ge samples were prepared from high-purity components (Pr > 99.9 and Ge > 99.999 wt.%) by arc melting under an argon atmosphere; the weight losses were less than 2 wt.%. The alloys were consecutively annealed in evacuated silica tubes at 873 K for 30 days and quenched into cold water.

Preliminary phase analysis was carried out based on diffraction patterns recorded with a Debye-Scherrer camera (diameter 53.7 mm) using Cr K radiation. The unit cell parameters were refined on X-ray diffraction data from polycrystalline samples, recorded on a diffractometer DRON-2.0 (Fe K $\alpha$  radiation,  $\lambda = 1.93735$  Å, internal silicon standard). The programs POWDER CELL [18] and LATCON [19] were used for the calculations.

Single crystals of Pr<sub>4</sub>Ge<sub>7</sub> were selected from a ternary alloy of nominal composition Pr<sub>33.3</sub>Al<sub>6.7</sub>Ge<sub>60</sub>.

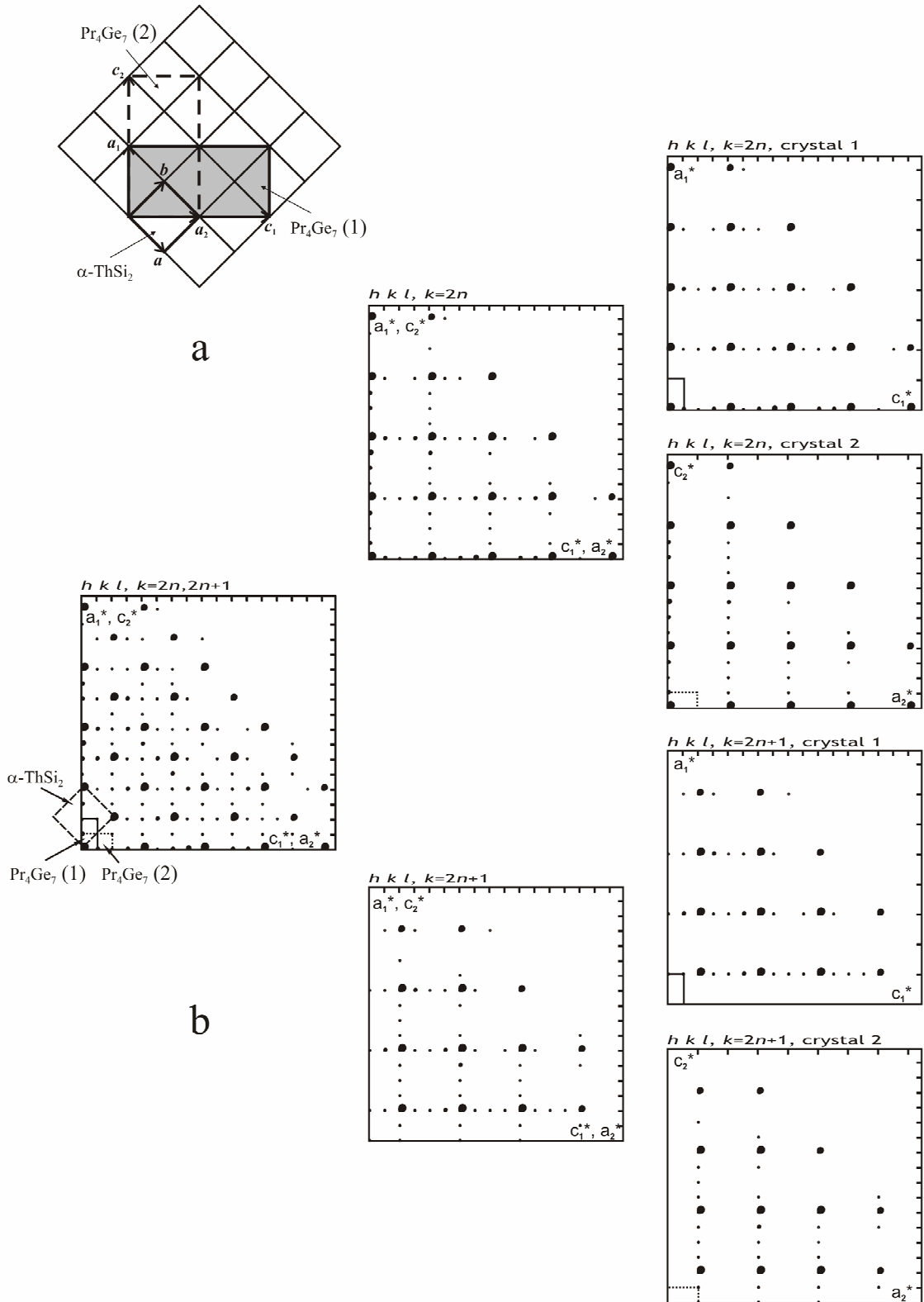
6382 reflections indexed on a pseudotetragonal cell 12.01×12.01×13.99 Å were collected on an Enraf-Nonius CAD-4 automatic diffractometer. Refinement in an α-ThSi<sub>2</sub> structure type subcell gave ~1/8 vacancies on the Ge site. No satisfactory model could be refined for the cell mentioned above. A more detailed analysis led to the conclusion that the true unit cell is smaller (6.007(2)×12.009(4)×13.987(4) Å). Fig. 1 shows that the diffraction pattern can be explained considering twinning where the unit cell vectors of the crystallites correlate via the matrix:

$$\begin{vmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{vmatrix}.$$

The study of possible group-subgroup relationships starting from the α-ThSi<sub>2</sub> type (space group *I4<sub>1</sub>/amd*) led to a model in space group *C222<sub>1</sub>* for the new unit cell (Table 2). This model was identical with the structure reported for Nd<sub>4</sub>Ge<sub>7</sub> [12]. The twinning corresponds to ordering of vacancies on the Ge sites in two mutually perpendicular directions with respect to the small tetragonal cell of the parent structure. For the refinement, equal contributions of both twins were considered. The program used to refine the structure was from SHELX-97 [20]. Structure data and details concerning the data collection and structure refinement are given in Table 3.

**Table 1** Crystallographic parameters of binary compounds in the Pr-Ge system (selected literature data from [4] and results of this work).

Ge content (at.%)	Compound	Structure type	Space group	Pearson symbol	Cell parameters (Å)			Reference
					<i>a</i>	<i>b</i>	<i>c</i>	
25.0	Pr <sub>3</sub> Ge	Ti <sub>3</sub> P	<i>P4<sub>2</sub>/n</i>	<i>tP32</i>	12.422	–	6.118	[5]
					12.418(5)	–	6.133(2)	[6]
37.5	Pr <sub>5</sub> Ge <sub>3</sub>	Mn <sub>5</sub> Si <sub>3</sub>	<i>P6<sub>3</sub>/mcm</i>	<i>hP16</i>	8.84	–	6.63	[2]
					8.801(2)	–	6.659(3)	this work
42.7	Pr <sub>4</sub> Ge <sub>3</sub>	Th <sub>3</sub> P <sub>4</sub>	<i>I<math>\bar{4}</math>3d</i>	<i>cI28</i>	9.32	–	–	[2]
					9.1460(6)	–	–	this work
44.4	Pr <sub>5</sub> Ge <sub>4</sub>	Sm <sub>5</sub> Ge <sub>4</sub>	<i>Pnma</i>	<i>oP36</i>	7.9141	15.1829	8.0060	[7]
					7.945(7)	15.199(8)	7.951(7)	this work
50.0	PrGe	CrB	<i>Cmcm</i>	<i>oS8</i>	4.480	11.092	4.054	[8]
					4.486(4)	11.09(1)	4.066(9)	this work
50.0	PrGe	FeB	<i>Pnma</i>	<i>oP8</i>	8.294	4.053	5.982	[8]
					8.301(4)	4.053(2)	5.962(4)	this work
61.5	β-PrGe <sub>1.6</sub>	α-ThSi <sub>2</sub>	<i>I4<sub>1</sub>/amd</i>	<i>tI12</i>	4.43	–	14.00	[2]
61.5	α-PrGe <sub>1.6</sub>	α-GdSi <sub>2</sub>	<i>Imma</i>	<i>oI12</i>	4.27	4.18	14.22	[2]
61.5	PrGe <sub>1.60</sub> (60 K)	Y <sub>3</sub> Ge <sub>5</sub>	<i>Fdd2</i>	<i>oF64</i>	5.9193	17.7582	14.128	[9]
61.5	PrGe <sub>1.60</sub> (Q <sub>1</sub> )	Y <sub>3</sub> Ge <sub>5</sub>	<i>Fdd2</i>	<i>oF64</i>	5.928	17.785	14.07	[10]
61.5	PrGe <sub>1.60</sub> (Q <sub>2</sub> )	α-ThSi <sub>2</sub>	<i>I4<sub>1</sub>/amd</i>	<i>tI12</i>	4.228	–	14.00	[10]
61.2	PrGe <sub>1.58</sub> (Q <sub>1</sub> )				4.201	–	14.101	[11]
60.0-61.8	PrGe <sub>1.50-1.62</sub>	α-ThSi <sub>2</sub>	<i>I4<sub>1</sub>/amd</i>	<i>tI12</i>	4.1980(1)-	–	14.131(3)-	this work
					4.2037(6)	–	14.093(5)	
62.1	ε'-PrGe <sub>1.64</sub>		<i>orthorhombic</i>		5.929	5.930	14.139	[12]
62.5	α'-Pr <sub>3</sub> Ge <sub>5</sub>	Y <sub>3</sub> Ge <sub>5</sub>	<i>Fdd2</i>	<i>oF64</i>	5.937	17.817	14.111	[12]
					5.992	14.003	12.002	[12]
63.6	β'-Pr <sub>4</sub> Ge <sub>7</sub>	Nd <sub>4</sub> Ge <sub>7</sub>	<i>C222<sub>1</sub></i>	<i>oS44</i>	6.007(2)	13.987(4)	12.009(4)	this work
					6.024	6.021	13.966	
63.9	γ'-PrGe <sub>1.77</sub>		<i>orthorhombic</i>		6.018	6.022	13.978	[12]
63.9	δ'-PrGe <sub>1.77</sub>		<i>orthorhombic</i>		6.018	6.022	13.978	[12]
64.3	PrGe <sub>1.8</sub> (Q <sub>2</sub> )				4.248	–	14.001	[11]
62.7-64.4	PrGe <sub>1.68-1.81</sub>	α-ThSi <sub>2</sub>	<i>I4<sub>1</sub>/amd</i>	<i>tI12</i>	4.243(1)-	–	14.010(6)-	this work
					4.260(1)	–	13.965(2)	
65.6	PrGe <sub>1.91</sub>	PrGe <sub>1.91</sub>	<i>Cmcm</i>	<i>oS36</i>	4.2721(6)	30.673(4)	4.1433(6)	[13]



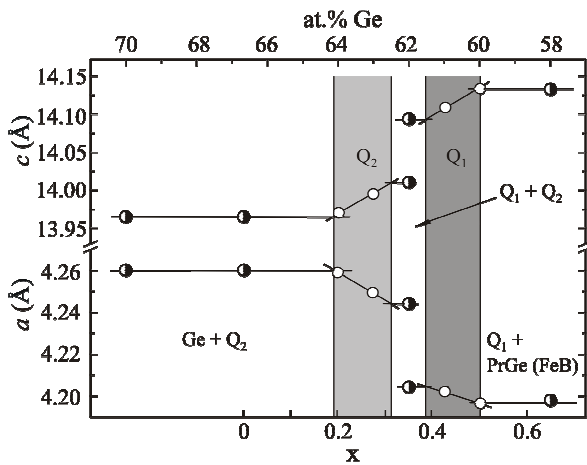
**Fig. 1** Relative orientation of the twins in the crystal used for the refinement of the structure of  $\text{Pr}_4\text{Ge}_7$  (a) and decomposition of the diffraction pattern into contributions from crystal 1 and crystal 2 (b).

**Table 2** Group-subgroup relationship between the structures of  $\alpha$ -ThSi<sub>2</sub> (I) and Pr<sub>4</sub>Ge<sub>7</sub> (V) (site Ge(5) is vacant).

Model	I	II	III	IV	V
Transformation matrix		1 0 0 0 1 0 0 0 1	1 1 0 -1 1 0 0 0 1	-1 1 0 0 0 1 1 1 0	-1 1 0 0 0 1 2 2 0
Space group	<i>I</i> <sub>4</sub> / <i>amd</i>	<i>I</i> <sub>4</sub> 22	<i>F</i> 222	<i>C</i> 222	<i>C</i> 222 <sub>1</sub>
Cell parameters (Å)	$a_I=4.260$ ( $b_I=a_I=4.260$ ) $c_I=13.965$	$a_{II}=a_I=4.260$ ( $b_{II}=a_I=4.260$ ) $c_{II}=c_I=13.965$	$a_{III}=\sqrt{2} a_I=6.025$ $b_{III}=\sqrt{2} a_I=6.025$ $c_{III}=c_I=13.965$	$a_{IV}=\sqrt{2} a_I=6.025$ $b_{IV}=c_I=13.965$ $c_{IV}=\sqrt{2} a_I=6.025$	$a_V=\sqrt{2} a_I=6.025$ $b_V=c_I=13.965$ $c_V=2\sqrt{2} a_I=12.050$
Site, Wyckoff position, atom coordinates	Pr 4a 0 $\frac{3}{4}$ $\frac{1}{8}$	Pr 4a 0 0 0	Pr(1) 4c $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$	Pr(1) 4k $\frac{1}{4}$ $\frac{1}{4}$ 0.2500	Pr(1) 8c 0.2500 0.2500 0.3750
			Pr(2) 4a 0 0 0	Pr(2) 2c $\frac{1}{2}$ 0 $\frac{1}{2}$	Pr(2) 4b 0 0.5000 $\frac{1}{4}$
	Ge 8e 0 $\frac{1}{4}$ 0.2915	Ge 8c 0 0 0.4165	Ge(1) 8h $\frac{1}{4}$ $\frac{1}{4}$ 0.6665	Ge(1) 8l 0.2500 0.6665 0.2500	Ge(2) 8c 0.2500 0.1665 0.1250 Ge(3) 8c 0.2500 0.3335 0.1250
			Ge(2) 8g 0 0 0.4165	Ge(2) 4g 0 0.4165 0 Ge(3) 4h 0 0.0835 $\frac{1}{2}$	Ge(1) 8c 0.0000 0.4165 0.0000 Ge(4) 4b 0 0.0835 $\frac{1}{4}$ Ge(5) 4b 0 0.9165 $\frac{1}{4}$

## Results and discussion

Crystallographic data for the binary Pr-Ge phases as determined in this work are included in Table 1. Nine germanides, Pr<sub>3</sub>Ge, Pr<sub>5</sub>Ge<sub>3</sub>, Pr<sub>4</sub>Ge<sub>3</sub>, Pr<sub>5</sub>Ge<sub>4</sub>, PrGe (CrB), PrGe (FeB), PrGe<sub>2-x</sub> (Q<sub>1</sub>), PrGe<sub>2-x</sub> (Q<sub>2</sub>), and PrGe<sub>1.91</sub>, were observed in the binary alloys annealed at 873 K. The cell parameters and homogeneity ranges of the non-stoichiometric digermanides PrGe<sub>2-x</sub> Q<sub>2</sub>



**Fig. 2** Cell parameters corresponding to the  $\alpha$ -ThSi<sub>2</sub> type and homogeneity ranges of the non-stoichiometric praseodymium digermanides Q<sub>2</sub> and Q<sub>1</sub>.

( $0.19 < x < 0.32$ , 64.4-62.7 at.% Ge) and Q<sub>1</sub> ( $0.38 < x < 0.50$ , 61.8-60.0 at.% Ge), shown in Fig. 2, are close to those reported in [11].

Fractional atom coordinates and anisotropic displacement parameters for Pr<sub>4</sub>Ge<sub>7</sub> (Pearson symbol *o*S44, space group C222<sub>1</sub>) are presented in Table 4. The refinement showed no indication for the presence of Al in the structure or for any deviation from an ordered arrangement of vacancies. The positional parameters were standardized with the program STRUCTURE TIDY [21]. The anisotropic displacement parameters of sites Ge(3) and Ge(4) show relatively large values, the corresponding ellipsoids being elongated in the direction towards the vacant Ge site. The shortest interatomic distances, listed in Table 5, are in agreement with usual values observed for Pr-Pr, Pr-Ge, and Ge-Ge distances.

Fig. 3 shows a projection of the structure of Pr<sub>4</sub>Ge<sub>7</sub>, along the shortest translation vector, [100]. The translation unit *b* corresponds to the *c*-parameter of the parent structure  $\alpha$ -ThSi<sub>2</sub>. As in the parent structure, each Ge site is surrounded by six Pr atoms forming a trigonal prism. The prisms exhibit minor distortions, and the centering Ge atoms are displaced from the prism center, leading to Ge-Pr distances ranging from 3.06 to 3.63 Å in the case of site Ge(3).

The structure type  $\alpha$ -ThSi<sub>2</sub> is characterized by a 3D-framework of Si-Si contact distances, where each Si atom is surrounded by three other Si atoms. Hexagons appear in the projection of the framework

formed by the majority element, shown in Fig. 4. The absence of 1/8 of the Ge atoms in Pr<sub>4</sub>Ge<sub>7</sub> with respect to the  $\alpha$ -ThSi<sub>2</sub> type causes interruptions in the framework, but the 3D-character of the Ge substructure is preserved. It can be seen from Fig. 4 that part of the hexagons present in the projection of the parent type remain. This is not the case in the related vacancy derivative Y<sub>3</sub>Ge<sub>5</sub> (space group *Fdd2*), where 1/6 of the Ge positions are vacant. The list of interatomic distances in Table 5 confirms that the sites Ge(1) and Ge(2) in Pr<sub>4</sub>Ge<sub>7</sub> have as nearest neighbors three other Ge atoms at distances 2.43-2.66 Å,

whereas the sites Ge(3) and Ge(4) have only two Ge atoms at similar distances.

Table 6 groups several partly or fully ordered vacancy derivatives of  $\alpha$ -ThSi<sub>2</sub>. In all these structures the construction of fused trigonal prisms formed by the large atoms remains. The types are ordered according to increasing amount of empty prism centers. No As-As contact distances exist in the structure type NbAs, where second *M* (As) position is vacant. An extended discussion about vacancy derivatives of  $\alpha$ -ThSi<sub>2</sub> can be found in the works by Venturini *et al.* [12,15].

**Table 3** Crystal data and details of the data collection and refinement for Pr<sub>4</sub>Ge<sub>7</sub>.

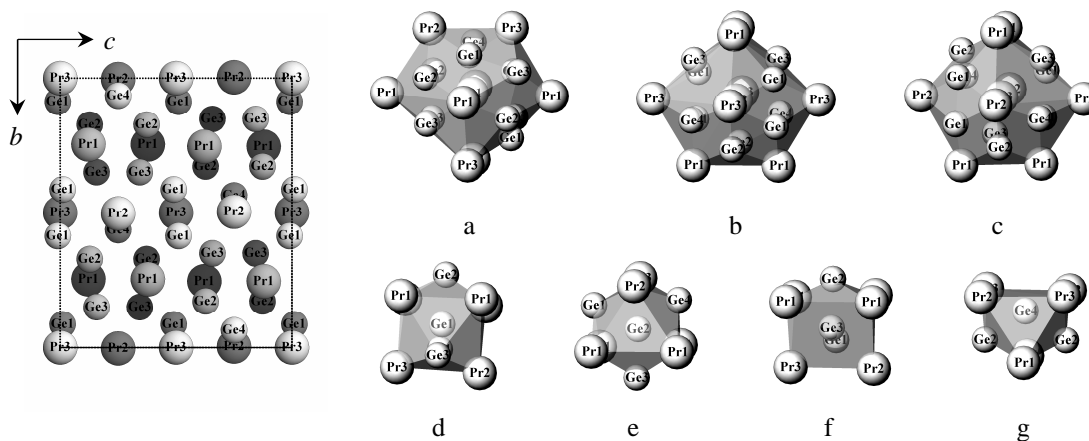
Nominal composition of the sample	Pr <sub>33.3</sub> Al <sub>6.7</sub> Ge <sub>60</sub>
Mass per formula unit $M_r$	1071.8
Space group	<i>C222</i> <sub>1</sub> (#20)
Cell parameters	
$a$ (Å)	6.007(2)
$b$ (Å)	13.987(4)
$c$ (Å)	12.009(4)
Cell volume $V$ (Å <sup>3</sup> )	1009.0(4)
Formula units per unit cell $Z$	4
Density $D_x$ (Mg·m <sup>-3</sup> )	7.055
Radiation, wavelength (Å)	Mo <i>K</i> $\alpha$ , 0.71073
Temperature for data collection (K)	293
Crystal size (mm)	0.025×0.035×0.045
Crystal color	gray, metallic
Scan method	$\omega$ -2 $\theta$
Absorption correction	empirical ( $\psi$ -scans)
Transmission factors $T_{\min}$ - $T_{\max}$	0.590-1.000
Number of measured reflections	2672
Number of independent reflections, $R_{\text{int}}$	651, 0.112
Limit for data collection $\theta_{\max}$ (°)	30
Range of indexes	
$h$	0→8
$k$	-19→19
$l$	0→16
Refinement on	$F$
Reliability factors	
$R$	0.110
$wR$	0.057
Number of refined parameters	54
Extinction coefficient	$1.2(1)\times 10^{-4}$

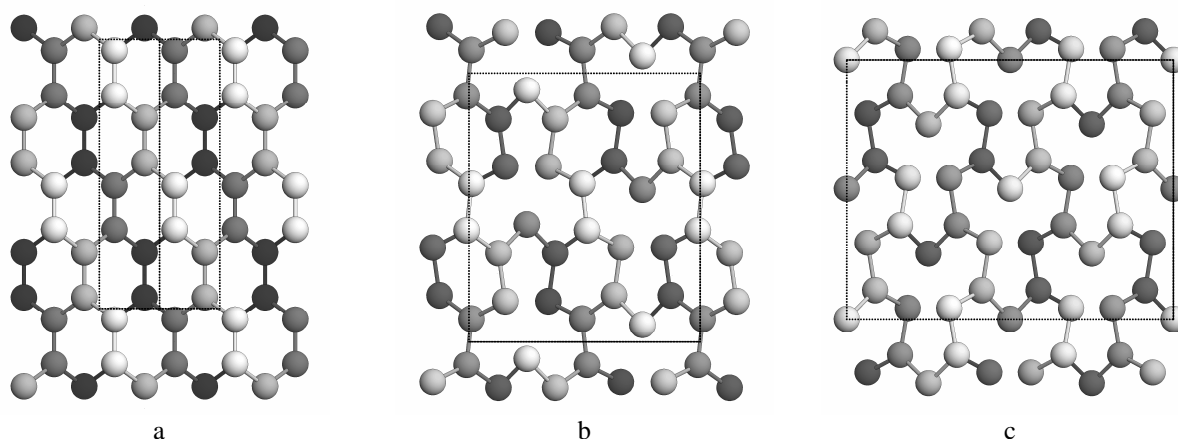
**Table 4** Fractional atomic coordinates and anisotropic displacement parameters (Å<sup>2</sup>) in the structure of Pr<sub>4</sub>Ge<sub>7</sub> (*C222*<sub>1</sub>,  $a = 6.007(2)$ ,  $b = 13.987(4)$ ,  $c = 12.009(4)$  Å).

Site	Wyckoff position	$x$	$y$	$z$	$U_{11}$	$U_{22}$	$U_{33}$	$U_{12}$	$U_{13}$	$U_{23}$
Pr(1)	8 <i>c</i>	0.2377(6)	0.2461(1)	0.3782(1)	0.014(2)	0.004(1)	0.004(2)	-0.001(1)	-0.001(1)	-0.003(1)
Pr(2)	4 <i>b</i>	0	0.5034(4)	¼	0.004(2)	0.008(1)	0.007(2)	0	-0.002(1)	0
Pr(3)	4 <i>a</i>	0.0087(7)	0	0	0.004(2)	0.010(1)	0.007(2)	0	0	0.003(1)
Ge(1)	8 <i>c</i>	0.016(1)	0.4135(3)	0.0105(5)	0.005(3)	0.005(2)	0.006(3)	-0.003(2)	0.005(3)	-0.002(2)
Ge(2)	8 <i>c</i>	0.2513(7)	0.1721(3)	0.1272(3)	0.004(2)	0.015(2)	0.004(2)	-0.003(1)	0.001(2)	0.004(1)
Ge(3)	8 <i>c</i>	0.313(1)	0.3493(4)	0.1567(6)	0.043(4)	0.027(3)	0.034(4)	0.025(3)	0.037(3)	0.024(3)
Ge(4)	4 <i>b</i>	0	0.0642(5)	¼	0.013(3)	0.039(4)	0.015(4)	0	-0.003(4)	0

**Table 5** Interatomic distances (Å) in the structure of Pr<sub>4</sub>Ge<sub>7</sub>.

Pr(1)	- 1 Ge(3)	3.060(6)	Pr(2)	- 2 Ge(3)	3.072(6)	
	- 1 Ge(3)	3.089(7)		- 2 Ge(4)	3.122(3)	
	- 1 Ge(1)	3.097(5)		- 2 Ge(1)	3.140(6)	
	- 1 Ge(1)	3.114(6)		- 2 Ge(2)	3.158(5)	
	- 1 Ge(2)	3.115(5)		- 2 Ge(1)	3.339(6)	
	- 1 Ge(2)	3.188(5)		- 2 Pr(1)	4.047(3)	
	- 1 Ge(2)	3.202(4)		- 2 Pr(1)	4.167(3)	
	- 1 Ge(2)	3.240(6)		- 2 Pr(3)	4.210(3)	
	- 1 Ge(4)	3.299(6)		- 2 Pr(3)	4.284(3)	
	- 1 Ge(3)	3.614(6)		Pr(3)	- 2 Ge(3)	3.060(5)
	- 1 Ge(3)	3.634(7)			- 2 Ge(4)	3.134(2)
	- 1 Pr(3)	4.022(3)			- 2 Ge(1)	3.200(8)
	- 1 Pr(2)	4.047(3)			- 2 Ge(2)	3.203(4)
	- 1 Pr(3)	4.132(3)			- 2 Ge(1)	3.281(8)
	- 1 Pr(2)	4.167(3)			- 2 Pr(1)	4.022(3)
	- 2 Pr(1)	4.194(4)			- 2 Pr(1)	4.132(3)
- 1 Pr(1)	4.200(4)	- 2 Pr(2)	4.210(3)			
- 1 Pr(1)	4.406(4)	- 2 Pr(2)	4.284(3)			
Ge(1)	- 1 Ge(1)	2.433(9)	Ge(3)	- 1 Ge(2)	2.531(8)	
	- 1 Ge(2)	2.588(8)		- 1 Ge(1)	2.659(9)	
	- 1 Ge(3)	2.659(9)		- 1 Pr(1)	3.060(6)	
	- 1 Pr(1)	3.097(5)		- 1 Pr(3)	3.060(5)	
	- 1 Pr(1)	3.114(6)		- 1 Pr(2)	3.072(6)	
	- 1 Pr(2)	3.140(6)		- 1 Pr(1)	3.089(7)	
	- 1 Pr(3)	3.200(8)		- 1 Pr(1)	3.614(6)	
	- 1 Pr(3)	3.281(8)		- 1 Pr(1)	3.634(7)	
Ge(2)	- 1 Ge(3)	2.531(8)	Ge(4)	- 2 Ge(2)	2.569(6)	
	- 1 Ge(4)	2.569(6)		- 2 Pr(2)	3.122(3)	
	- 1 Ge(1)	2.588(8)		- 2 Pr(3)	3.134(2)	
	- 1 Pr(1)	3.115(5)		- 2 Pr(1)	3.299(6)	
	- 1 Pr(2)	3.158(5)				
	- 1 Pr(1)	3.188(5)				
	- 1 Pr(1)	3.202(4)				
	- 1 Pr(3)	3.203(4)				
- 1 Pr(1)	3.240(6)					

**Fig. 3** Projection of the structure of Pr<sub>4</sub>Ge<sub>7</sub> along [100] and coordination polyhedra: Pr(1)Ge<sub>11</sub>Pr<sub>8</sub> (a), Pr(2)Ge<sub>10</sub>Pr<sub>8</sub> (b), Pr(3)Ge<sub>10</sub>Pr<sub>8</sub> (c), Ge(1)Pr<sub>6</sub>Ge<sub>3</sub> (d), Ge(2)Pr<sub>6</sub>Ge<sub>3</sub> (e), Ge(3)Pr<sub>6</sub>Ge<sub>2</sub> (f), Ge(4)Pr<sub>6</sub>Ge<sub>2</sub> (g).



**Fig. 4** Projections of the framework formed by the majority element in the structures of  $\alpha$ -ThSi<sub>2</sub> (a), Pr<sub>4</sub>Ge<sub>7</sub> (b) and Y<sub>3</sub>Ge<sub>5</sub> (c).

**Table 6** Simple vacancy derivatives  $RM_{2-x}$  of the  $\alpha$ -ThSi<sub>2</sub> structure type.

x	Structure type	Space group	Pearson symbol	Translation vectors with respect to $\alpha$ -ThSi <sub>2</sub>			Reference
				<b>a</b>	<b>b</b>	<b>c</b>	
0	$\alpha$ -ThSi <sub>2</sub>	$I4_1/amd$	$tI12$	<b>a</b>	<b>b</b>	<b>c</b>	[22]
0.25	Nd <sub>4</sub> Ge <sub>7</sub>	$C222_1$	$oS44$	<b>-a + b</b>	<b>c</b>	$2(\mathbf{a} + \mathbf{b})$	[12]
0.25	ThNi <sub>1.75</sub>	$C2/c$	$mS12-1$	<b>a + b</b>	<b>-a + b</b>	$(-\mathbf{a} - \mathbf{b} + \mathbf{c})/2$	[23]
0.33	Y <sub>3</sub> Ge <sub>5</sub>	$Fdd2$	$oF64$	<b>-a + b</b>	$3(\mathbf{a} + \mathbf{b})$	<b>c</b>	[14]
0.39	CeGe <sub>0.66</sub> Si <sub>0.95</sub>	$I\bar{4}m2^a$	$tI12-1.56$	<b>a</b>	<b>b</b>	<b>c</b>	[24]
0.44	Ce <sub>9</sub> Ge <sub>14</sub>	$I4_1$	$tI104-12$	$3\mathbf{a}$	$3\mathbf{b}$	<b>c</b>	[25]
0.60	$\alpha$ -GdSi <sub>1.4</sub>	$Imma$	$oI12-2.4$	<b>a</b>	<b>b</b>	<b>c</b>	[26]
1	NbAs	$I4_1md$	$tI8$	<b>a</b>	<b>b</b>	<b>c</b>	[27]

<sup>a</sup> originally reported in space group  $F222$  (see [4])

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